

OLD DOMINION UNIVERSITY COLLEGE OF SCIENCES

Math 162

Skill Blasters

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Skills Blaster Program for Math 162 Precalculus Created for the Math and Science Resource Center Prepared by Kele McKaig Old Dominion University 2017

Content Structure:

Each week Skills Blaster worksheets will be distributed to students in Precalculus (Math 162). The worksheets will contain 3 Math problems covering the fundamental skills necessary for students to successfully complete the topic that will be presented in the lecture course the following week. The Skills Blaster worksheets will be structured as follows:

Topic: Math content to be covered in lecture the following week.

Questions to reflect upon: Discussion of the skills necessary to understand and engage with the Math content that will be presented in class the following week.

Demonstration of problem: Example problem worked out to completion.

Evaluate: 3 questions for the student to evaluate PRIOR to the Skills Blaster session.

Notes: Section for students to write questions and notes they have related to the material presented on the Skills Blaster worksheet.

Course Structure:

The weekly Skills Blaster worksheets will be delivered to the students in Math 162 through their lecture course on Blackboard. The worksheets are to be completed **PRIOR** to the Skills Blaster session meeting time. The Skills Blaster session will begin by welcoming the students to the meeting. The leader of the Skills Blaster session will then review the problems that the students completed prior to the session and poll the students to see if there are any questions. The meeting shall continue until either all questions are exhausted, or until the end of the scheduled meeting time. *Note: Attendance should be taken and reported to the Math lecturers, in the case of students receiving extra credit.* The answers to the Skills Blaster session. *Note: The answers should also be distributed to the lecturers in Math 162 to post on Blackboard after the session time.*

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Intended Schedule

Week	Lecture Topic	Skill Blaster Area of Focus
1	Linear Equations in One Variable	Adding and Subtracting Fractions
2	Linear Equations in Two Variables	Solving Squared and Cubed Equations
3	Quadratic Equations	Solving Inequality Equations
4	Inequalities and Absolute Values	Interval Notation
5	Graphing Equations	Plotting Points on Graph
6	Functions	Solving for f(x) given f(a)
7	Transformations of Functions	Finding f(-x) and -f(x)
8	Composite and Inverse Functions	Solving An Equation for a Specific Variable
9	Quadratic Functions	Finding X and Y Intercepts
10	Polynomials Functions and Real Zeros	Laws of Exponents
11	Rational Functions	Simplify Complex Fractions
12	Exponential Functions	Simplify Fractions with Radicals
13	Logarithmic Functions and Rules of Logarithms	Thanksgiving Break
14	Partial Fraction Decomposition	Solving Rational Equations
15	Complex Zeros of Polynomial Functions	Encourage Participation in Exam Jams

*Highlighted weeks are worksheets also used for M103.

Suggested worksheets:

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Skill Blaster for Precalculus MATH162

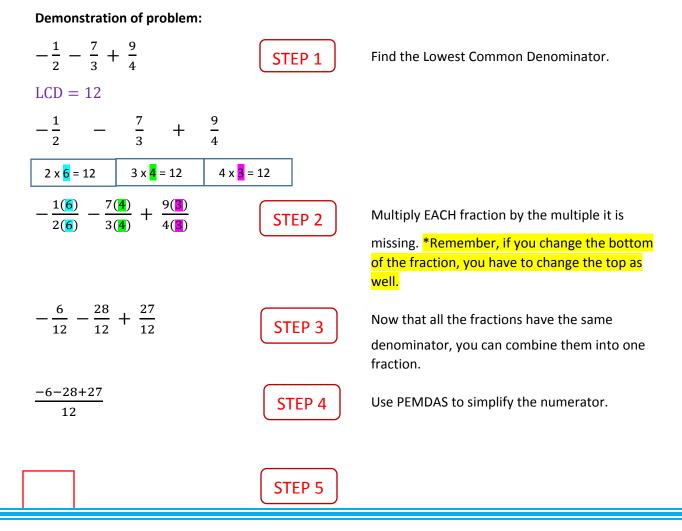
Week One

Topic: Linear Equations in One Variable

Questions to reflect upon: Do you know what PEMDAS stands for? Do you fully understand fundamental mathematical operations of addition, subtraction, multiplication and division? Do you know how to add or subtract fractions?

Problem:

$$-\frac{1}{2}-\frac{7}{3}+\frac{9}{4}$$





*Always check if your answer can reduce!

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

1.
$$\frac{10}{4} - \frac{4}{3} + \frac{1}{4}$$

2. $-\frac{8}{7} + \frac{1}{2} - \frac{4}{14}$
3. $\frac{1}{2} + \frac{2}{6} + \frac{6}{4} - \frac{1}{2}$

2

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Topic: Linear Equations in Two Variables

Questions to reflect upon: Do you know how to solve squared and cubed equations? Problem:

1.
$$(x+2)^2 = 9$$

Demonstration of problem:

$(x+2)^2 = 9$ $\sqrt{(x+2)^2} = \sqrt{9}$ $x+2 = \pm 3$	STEP 1	The first step in isolating the variable is taking care of the exponent. Because the expression $(x + 2)$ is raised to the second power, we have to take the square root of both sides to remove it.
Thus:		*Remember! Taking an EVEN root means you have the possibility for both a positive and
x + 2 = 3		negative answer, so you MUST have two equations at this stage. THIS IS NOT THE CASE
x + 2 = -3		WITH ODD ROOTS! Odd roots would only produce one equation at this point.
x + 2 = 3 $x = 1$	STEP 2	Solve BOTH resulting equations.
x + 2 = -3 $x = -5$		



*Always check your answer by plugging it back into the original equation!

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

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1.
$$(x + 1)^2 = 25$$

2.
$$(2x-2)^2 = 16$$

3.
$$(x-4)^3 = 27$$

Notes:

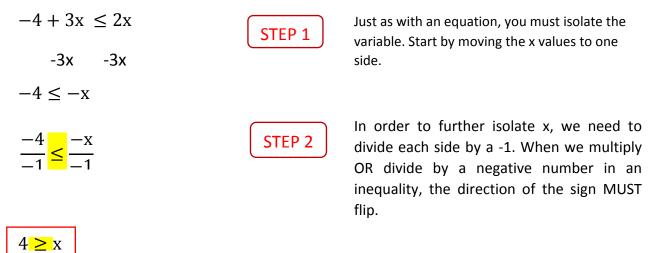
Math and Science Resource Center Skill Blaster for Precalculus MATH162 Week Three

Topic: Quadratic Equations

Questions to reflect upon: Do you know how to solve an Inequality Equation? Problem:

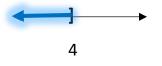
 $-4 + 3x \le 2x$

Demonstration of problem:



*Inequalities can also be expressed in a number line, as well as in interval notation:

Number line:



Interval Notation:

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

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1.
$$2 + 2x \le -5x$$

2. $3x + 9 \ge -2x - 1$

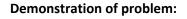
3.
$$4 \le -2x + 1 \le 10$$

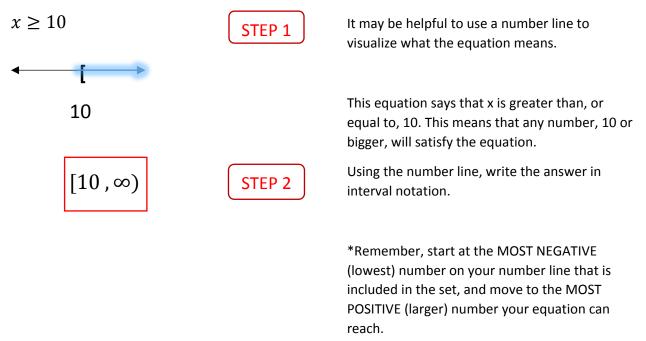
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Week Four	

Topic: Inequalities and Absolute Values

Questions to reflect upon: Do you know how to write an answer to an inequality in Interval Notation? **Problem:**

Write $x \ge 10$ in interval notation.





*Remember, inequalities with a bar underneath the sign, $\leq or \geq$, ALWAYS get a hard-bracket, [or]. Inequalities without this bar, < or >,get a normal parentheses, (or). Infinity signs, $- \infty or \infty$, ALWAYS get parentheses. **Evaluate:** Complete these three problems PRIOR to the Skill Blaster Session.

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Write the following inequalities in interval notation:

1. $x \le -3$

2. 7 < *x*

3. $4 < x \le 8$

Notes:		
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Topic: Graphing Equations

Questions to reflect upon: Do you know how to take a set of points and plot them on a graph? Do you know how to look at a graph and determine the ordered pair associated with a point?

Problem:

Plot the points (1, 2), (-4, -5), (-2, 1) and (1, -2)

Demonstration of problem:

(1,2) ↓↓ x y

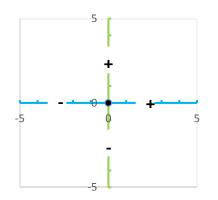
STEP 1

Understand that an ordered pair is a description of a point given as (x, y).

$$(-4, -5) \rightarrow x = -4, y = -5$$

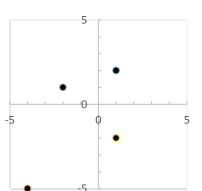
 $(-2, 1) \rightarrow x = -2, y = 1$

$$(1,-2) \rightarrow x = 1, y = -2$$





Understand the structure of a graph. The x axis is represented as the horizontal axis while the y axis is represented as the vertical axis. The point where the two axes cross is the origin where both x and y are zero. The left side of the horizontal axis becomes more negative, while the right side becomes more positive. The bottom portion of the vertical axis becomes more negative, while the upper portion becomes more positive.



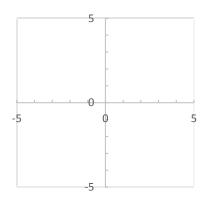
Now plot the points. Start by moving horizontally to the value of x, then up or down to the value of corresponding y.

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

• 5 Write out any questions for your Skill Blaster Instructor in the Notes section. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

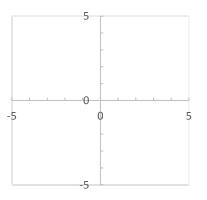
1. Plot the following points: (2,4), (-1,3), (3,4), (5,-1), (0,-1), (-2,0)

STEP 3

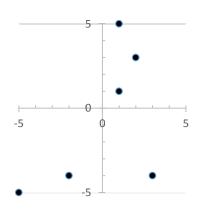


2. Plot the following points:

Х	Y
-2	-2
-1	-3
-4	5
2	3
2	-2



3. Identify the points in the graph as ordered pairs.



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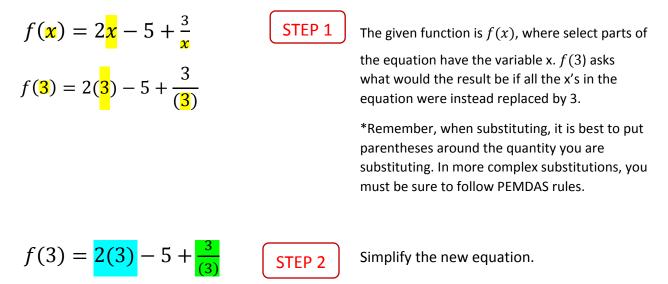
Topic: Functions

Questions to reflect upon: Do you know how to find f(a), given f(x)?

Problem:

Given
$$f(x) = 2x - 5 + \frac{3}{x}$$
 find $f(3)$

Demonstration of problem:



$$f(3) = 6 - 5 + 1$$
$$f(3) = 1 + 1$$
$$f(3) = 2$$

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

1. Given
$$f(x) = 4x - 1 + \frac{4}{x}$$
 find $f(2)$

2. Given
$$f(x) = \frac{3x}{2} - 7x + 1$$
 find $f(4)$

3. Given
$$f(x) = 2x - 5$$
 find $f(x + 1)$

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Topic: Transformations of Functions

Questions to reflect upon: Do you know how to find f(-x) and -f(x)?

Problem:

Given
$$f(x) = -4x + \frac{1}{x} - 1$$
 find $f(-x)$ and $-f(x)$

Demonstration of problem:

$$f(x) = -4x + \frac{1}{x} - 1$$

$$f(x) = -(-4x + \frac{1}{x} - 1)$$

$$f(-x) = -4(-x) + \frac{1}{(-x)}$$

$$f(-x) = -4(-x) + \frac{1}{(-x)}$$

$$STEP 1$$

$$-f(x) refers to making the entire f(x) negative, whereas f(-x) refers to replacing every x with -x
$$Remember, when substituting, it is best to put parentheses around the quantity you are substituting.
$$-f(x) = -(-4x + \frac{1}{x} - 1)$$

$$STEP 2$$
Simplify the equations.$$$$

$$-f(x) = 4x - \frac{1}{x} + 1$$
$$f(-x) = -4(-x) + \frac{1}{(-x)} - 1$$
$$f(-x) = 4x - \frac{1}{x} - 1$$

*It is important to note that -f(x) and f(-x) are NOT interchangeable, as seen above.

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

1. Given $f(x) = x - 1 + \frac{x}{2}$ find - f(x) and f(-x)

2. Given $f(x) = -7x^3 + 4(1 - x) + 1$ find -f(x) and f(-x)

3. Given
$$f(x) = 3x^2 - 5x + 7$$
 find find $- f(x)$ and $f(-x)$

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Week Eight

Topic: Composite and Inverse Functions

Questions to reflect upon: Do you know how to solve an equation for a specific variable? **Problem:**

Solve
$$4x = \frac{y-1}{3y+2z}$$
 for y

Demonstration of problem:

$$4x = \frac{y-1}{3y+2z}$$
Identify the variable you are solving for and

$$(3y + 2z) * 4x = \frac{y-1}{3y+2z} * (3y + 2z)$$

$$4x(3y + 2z) = y - 1$$
Identify the variable you are solving for and
determine what portion of the equation to
move first. As one of the y terms is in the
denominator of a fraction, the first move should
be eliminating that fraction by multiplying to
both sides.
*Because there are two terms, you CANNOT
just multiply by one of the terms.
In order to get the y value out of the
parentheses, the left side needs to be

distributed.

4x(3y+2z) = y-1

$$12xy + 8xz = y - 1$$
$$12xy - y = -8xz - 1$$

y(12x - 1) = -8xz - 1

Now, you must get all the terms that contain a y on one side, and move everything else to the other.

Because each term on the left hand side contains a y, you can factor the y out of each term. Then, in order to isolate y, you can divide out the rest.

$$\frac{y(12x-1)}{(12x-1)} = \frac{-8xz-1}{(12x-1)}$$
$$y = \frac{-8xz-1}{12x-1}$$

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

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STEP 3

1. Solve
$$2z = \frac{x-1}{x+2y}$$
 for x

2. Solve
$$4 = \frac{y-1}{y+2}$$
 for y

3. Solve
$$x + 2 = \frac{y - 3z}{3y + 2z}$$
 for y

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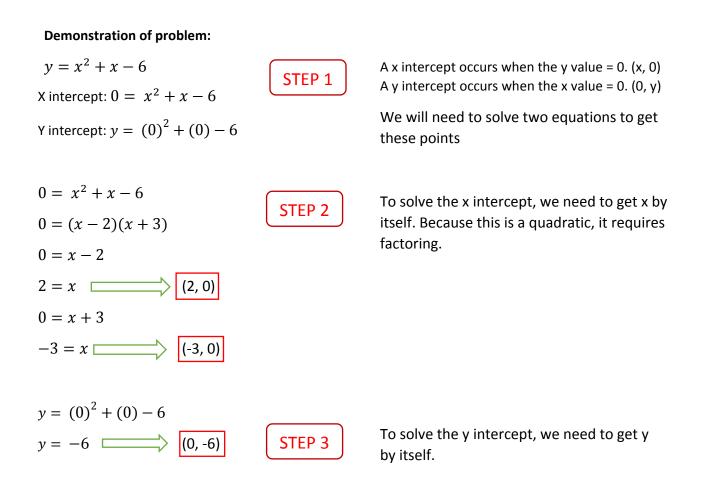
Week Nine

Topic: Quadratic Functions

Questions to reflect upon: Do you know how to find X and Y intercepts?

Problem:

Find the x and y intercept of $y = x^2 + x - 6$.



Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

Find the x and y intercept of the following equations:

1.
$$y = 2x^2 + 2x - 4$$

2.
$$y = 3x^2 - 6$$

3.
$$3x + 2y = 4$$

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Week Ten

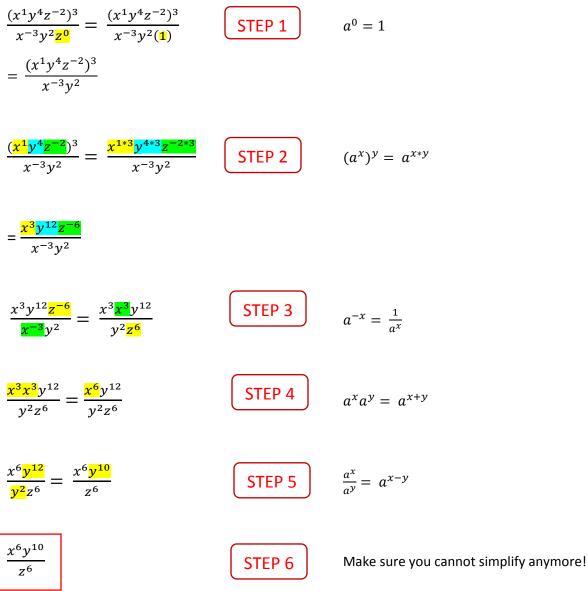
Topic: Polynomials Functions and Real Zeros

Questions to reflect upon: Do you know the laws of exponents?

Problem:

Simplify
$$\frac{(x^1y^4z^{-2})^3}{x^{-3}y^2z^0}$$
 using the laws of exponents.

Demonstration of problem:



Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

1. Simplify
$$\frac{(x^3y^2z^1)^2}{x^2y^4z^1}$$

2. Simplify
$$\frac{x^{-2}y^{-2}}{(x^{-3}y^{-2}z^4)^4}$$

3. Simplify
$$\frac{(x^{-4}y^{-3})^{-2}}{(y^{-2}z^1)^{-1}}$$

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Topic: Rational Functions

Questions to reflect upon: Do you know how to find an LCD involving variable expressions in the denominator?

Problem:

Simplify the expression
$$\frac{2}{3x} + \frac{1}{x+1} - \frac{3}{3}$$
 into one fraction.

Demonstration of problem:

$$\frac{2}{3x} + \frac{1}{x+1} - \frac{5}{3}$$
STEP 1Find the Lowest Common Denominator.LCD = 3x(x+1) *Remember, the LCD is all the factors that make up the denominators! $\frac{2(x+1)}{3x(x+1)} + \frac{1(3x)}{(x+1)(3x)} - \frac{5(x(x+1))}{3(x(x+1))}$ STEP 2Multiply EACH fraction by the multiple it is
missing. Pay attention to the number of terms
in the denominators, and distribute as needed! $\frac{2x+2}{3x(x+1)} + \frac{3x}{3x(x+1)} - \frac{5(x^2+x)}{3x(x+1)}$ STEP 3Now that all the fractions have the same
denominator, you can combine them into one
fraction. $\frac{2x+2+3x-5(x^2+x)}{3x(x+1)}$ STEP 4Use PEMDAS to simplify the numerator.
*Remember, you cannot combine unlike terms. $\frac{2x+2+3x-5x^2-5x}{3x(x+1)}$ STEP 5*Always check if your answer can reduce! For a
fraction with MORE THAN ONE term in the
numerator, every term must be able to reduce
by the same factor!

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\frac{-3x^2+2}{3x(x+1)}
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Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

Simplify the expression into one fraction:

1.
$$\frac{1}{x+1} + \frac{2}{2} - \frac{4}{x}$$

2.
$$\frac{3}{2x} - \frac{1}{3x} - \frac{3}{x-4}$$

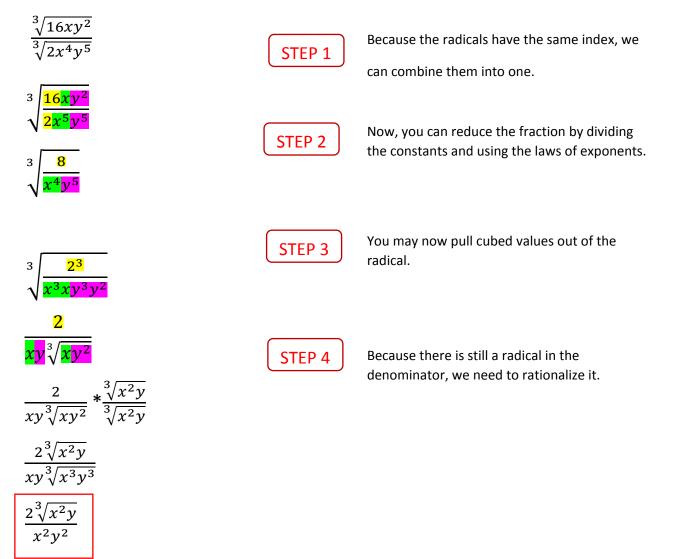
3.
$$\frac{x}{2x} + \frac{1}{12} + \frac{2}{3x} - \frac{2x}{2x-1}$$

Math and Science Resource Center Skill Blaster for Precalculus MATH162 Week Twelve **Topic:** Exponential Functions

Questions to reflect upon: Do you know how to simplify fractions with radicals?

Simplify
$$\frac{\sqrt[3]{16xy^2}}{\sqrt[3]{2x^5y^5}}$$

Demonstration of problem:



Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

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Simplify:

1.
$$\frac{\sqrt[3]{4x^2y^{10}}}{\sqrt[3]{24x^5y^6}}$$

2.
$$\frac{3x}{\sqrt[3]{27x^{13}y^2}}$$

$$3. \ \frac{4xy\sqrt{18x^4}}{\sqrt{2y^2}}$$

Notes:

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Week Thirteen

Topic: Add/Subtract/Multiply Radicals

Thanksgiving Break

Math and Science Resource Center Skill Blaster for Precalculus MATH162 Week Fourteen Topic: Partial Fraction Decomposition

Questions to reflect upon: Do you know how to solve rational equations? **Problem:**

$$\frac{12}{x^2 - 4} = \frac{1}{x - 2} + \frac{3}{x + 2}$$

Demonstration of problem:

$$\frac{12}{x^2-4} = \frac{1}{x-2} + \frac{3}{x+2}$$
STEP 1
The goal is to find an LCD to multiply the equation by that will eliminate the denominators. Simplify the denominators as much as possible by factoring where you can to determine the LCD.
$$(x-2)(x+2) * \frac{12}{(x-2)(x+2)} = (x-2)(x+2) * \frac{1}{x-2} + (x-2)(x+2) * \frac{3}{x+2}$$
12 = $(x+2) * 1 + (x-2) * 3$
STEP 2
The next step is to simplify the equation.
12 = $x + 2 + 3x - 6$
12 = $4x - 4$
STEP 3
Solve for x.
4 = x

$$\frac{12}{(4)^2-4} = \frac{1}{(4)-2} + \frac{3}{(4)+2}$$
STEP 4
You MUST check your answer with rational equations. If ANY of the denominators become zero, it means there is no solution!
 $x = 4$

Evaluate: Complete these three problems PRIOR to the Skill Blaster Session.

Write out any questions for your Skill Blaster Instructor in the Notes section below. If you encountered any difficulties or uncertainties with these problems, be sure to record where you encountered them and why you feel you struggled.

Solve the following:

1.
$$\frac{9}{x^2+3x+2} = \frac{1}{x+2} + \frac{2}{x+1}$$

2.
$$\frac{1}{x-4} + \frac{1}{x-2} = \frac{7}{(x-2)(x-4)}$$

$$3. \ \frac{6}{x-4} = \ \frac{1}{3} - \frac{3}{x}$$

Notes:

Math and Science Resource Center Skill Blaster for Precalculus MATH162 Week Fifteen **Final Preparation**